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#### **SPEAKERS**



Dr. David Brin (UCSD)





Prof. Brian Keating Dr. Andrew Friedman (UCSD) (MIT)





Massachusetts Institute of Technology

# OUTLINE



# Math: True in Any World

## OBSERVER SPACE AAST LIGHT CONF.

# Science: True in Our World



# Science and Spirituality



# The Mind of God

# MATH: INVENTED OR DISCOVERED?



# WHAT IS MATHEMATICAL TRUTH?



# Is the Pythagorean theorem always TRUE?

# **AXIOMS OF EUCLIDEAN GEOMETRY**

- 1. You can draw a straight line between any two points.
- 2. Straight lines can be extended forever in both directions.
- 3. Given any straight line segment, a circle can be drawn having the segment as radius and one endpoint as center.
- 4. All right angles are congruent.
- 5. parallel postulate. Given any straight line and a point not on it, there "exists one and only one straight line which passes" through that point and never intersects the first line, no matter how far they are extended.

 Weisstein, Eric W. "Euclid's Postulates." From MathWorld--A Wolfram Web Resource. http://mathworld.wolfram.com/EuclidsPostulates.html
 http://mathworld.wolfram.com/ParallelPostulate.html

 https://www.haikudeck.com/euclidean-ys-non-euclidean-geometry-education-presentation-cVKqsvE6eH#slide3
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## **NON-EUCLIDEAN GEOMETRY**

- 1. You can draw a straight line between any two points.
- 2. Straight lines can be extended forever in both directions.
- 3. Given any straight line segment, a circle can be drawn having the segment as radius and one endpoint as center.
- 4. All right angles are congruent.



 Weisstein, Eric W. "Euclid's Postulates." From MathWorld--A Wolfram Web Resource. http://mathworld.wolfram.com/EuclidsPostulates.html
 http://mathworld.wolfram.com/ParallelPostulate.html

 https://www.haikudeck.com/euclidean-vs-non-euclidean-geometry-education-presentation-cVKqsvE6eH#slide3
 http://wap.gsfc.nasa.gov/media/990006/990006\_2048.jpg
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# **CONDITIONAL MATHEMATICAL TRUTH** If axioms —> then theorems

If no "parallel" postulate



spherical geometry

hyperbolic geometry

True whether we like it or not.

Not even God could change this!

# MAP VS. TERRITORY

$$p_{G}(\lambda|x,y) = \frac{w}{4\pi} \left( \frac{1+\cos\alpha\,\operatorname{sign}\,[\cos\phi_{\lambda}\cos(\phi_{\lambda}-\alpha)]}{1+(1-2\alpha/\pi)\,\operatorname{sign}\,[\cos\phi_{\lambda}\cos(\phi_{\lambda}-\alpha)]} \right) + (1-w)\frac{|\sin\theta_{\lambda}\cos\phi_{\lambda}|}{2\pi}$$

$$p_{G}(\lambda|x',y) = \frac{w}{4\pi} \left( \frac{1+\cos(\beta-\alpha)\,\operatorname{sign}\,[\cos(\phi_{\lambda}-\beta)\cos(\phi_{\lambda}-\alpha)]}{1+(1-2(\phi_{\beta\alpha})/\pi)\,\operatorname{sign}\,[\cos(\phi_{\lambda}-\beta)\cos(\phi_{\lambda}-\alpha)]} \right) + (1-w)\frac{|\sin\theta_{\lambda}\cos(\phi_{\lambda}-\beta)|}{2\pi}$$

$$p_{G}(\lambda|x,y') = \frac{w}{4\pi} \left( \frac{1+\cos\gamma\,\operatorname{sign}\,[\cos\phi_{\lambda}\cos(\phi_{\lambda}-\gamma)]}{1+(1-2\gamma/\pi)\,\operatorname{sign}\,[\cos\phi_{\lambda}\cos(\phi_{\lambda}-\gamma)]} \right) + (1-w)\frac{|\sin\theta_{\lambda}\cos\phi_{\lambda}|}{2\pi}$$

$$p_{G}(\lambda|x',y') = \frac{w}{4\pi} \left( \frac{1+\cos(\beta-\gamma)\,\operatorname{sign}\,[\cos(\phi_{\lambda}-\beta)\cos(\phi_{\lambda}-\gamma)]}{1+(1-2(\phi_{\beta\gamma})/\pi)\,\operatorname{sign}\,[\cos(\phi_{\lambda}-\beta)\cos(\phi_{\lambda}-\gamma)]} \right) + (1-w)\frac{|\sin\theta_{\lambda}\cos(\phi_{\lambda}-\beta)|}{2\pi}$$







# **TESTING IF MATH IS DISCOVERED**

# Replay history billions of times!

# **TESTING IF MATH IS DISCOVERED**



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https://s-media-cache-ak0.pinimg.com/736x/fe/9d752/fe9d524c365c410f711c6e7679a3dc25.jpg

# WHY IS MATH SO GOOD AT SCIENCE?

"The unreasonable effectiveness of mathematics in the natural sciences" Wigner, 1960 igene drup (1,1,2,2) from ag e most i about the universe is that it is ensible" - Albert Einster

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![](_page_11_Picture_4.jpeg)

![](_page_11_Picture_5.jpeg)

![](_page_11_Picture_6.jpeg)

http://www.beamq.com/images/Most%20Powerful%20Blue%20Laser%202W.png

# **SCIENTIFIC TRUTH**

#### **Empirical Testing**

Question assumptions. Develop models. Make risky predictions. Do careful experiments.

#### **Explanation and Interpretation**

Find which mathematical models best explain the world. Give meaning to the mathematics.

#### **Error Correction**

Be aware of your own biases. Correct for them!

#### Humility and Open Mindedness

Parametrize our Ignorance. No perfect certainty. No Dogma. Knowledge is always provisional. Keep updating your beliefs based on new evidence.

#### THE MIND OF GOD

![](_page_13_Picture_1.jpeg)

# **DO YOU BELIEVE IN GOD?**

![](_page_14_Picture_1.jpeg)

# Not a YES or NO question! All the complexity gets hidden in the definition.

## **INADEQUACY OF RELIGIOUS LABELS**

![](_page_15_Picture_1.jpeg)

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# Struggler, skeptic, seeker, humanist, scientist?

#### **GOD IS NOT A PERSON**

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#### **AVOIDING A STERILE DEFINITION**

## Pantheism:

The view that everything is part of an all-encompassing immanent abstract God; or that the universe, or nature, and God are equivalent.

What's Missing:

Not Good Enough God=the universe God=the laws of physics God=mathematical truth A POSSIBLE DEFINITION OF GOD God is the collective knowledge and meaning created by all conscious beings in history of the universe.

God is an imperfect, continually evolving, open-ended process in the natural world.

The "Mind of God" is comprehensible by us.

But God is NOT A PERSON! Personhood only applies to living beings.

# HUMILITY AND RESPONSIBILITY The Meaning of Life, the Universe, and Everything?

# SCIENCE AND SPIRITUALITY

![](_page_20_Picture_1.jpeg)

The epitome of spirituality, for me, is doing science!

# CONCLUSIONS

![](_page_21_Picture_1.jpeg)

"Knowledge" part of God is objective. Out there to be discovered. Mathematical and scientific truth.

![](_page_21_Picture_3.jpeg)

"Meaning of life" part of God is subjective. Only we can invent and create it.

![](_page_21_Picture_5.jpeg)

The universe is comprehensible by us. If it wasn't, we wouldn't be here.

![](_page_21_Picture_7.jpeg)

Everyone must undergo their own struggle. Spiritual beliefs are our personal responsibility.

# CONCLUSIONS

![](_page_22_Picture_1.jpeg)

Carl Sagan: "We are the eyes and ears of the cosmos". The means by which an unconscious universe can come to understand itself.

![](_page_22_Picture_3.jpeg)

The cosmos was not created for us by a God that exists outside the universe. Nor are we the "center" of the universe.

![](_page_22_Picture_5.jpeg)

But the Copernican principle goes too far. Conscious beings ARE critically important in the cosmic scheme.

![](_page_22_Picture_7.jpeg)

Without us, nothing in the universe would matter. Without us, "the Mind of God" could never exist.

# **NEXT TALKS**

![](_page_23_Picture_1.jpeg)

The origin of Time in the universe

![](_page_23_Picture_3.jpeg)

https://upload.wikimedia.org/wikipedia/commons/a/ad/Astronomical\_Clock,\_Prague.jpg

![](_page_23_Picture_5.jpeg)

Science, Religion, and the Big Questions.

![](_page_23_Picture_7.jpeg)

http://www.rawstory.com/wp-content/uploads/2015/10/AngryGod-800x430.jpg

Dr. David Brin (UCSD)

#### REFERENCES

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Albert Einstein, Quoted in Timothy Ferris, "Coming of Age in the Milky Way", (New York, Morrow, 1988), p. 177.

Carl Sagan, "Pale Blue Dot: A Vision of the Human Future in Space", Random House (1994) p. 77.

Carl Sagan, "Cosmos", Random House, (1980), 396 pp (2013 edition)

Sean Caroll, "The Big Picture: On the Origins of Life, Meaning, and the Universe Itself", Dutton (2016), 480 pp

Eugene Wigner, "The Unreasonable Effectiveness of Mathematics in the Natural Sciences," in Communications in Pure and Applied Mathematics, vol. 13, No. I (February 1960). New York: John Wiley & 25

## **INDEPENDENT MATH DISCOVERY**

Logarithms – John Napier (Scotland, 1614) and Joost Bürgi (Switzerland, 1618).

Analytic geometry – René Descartes, Pierre de Fermat.

Problem of points solved by both Pierre de Fermat (France, 1654), Blaise Pascal (France, 1654), and Huygens (Holland, 1657).

Determinants – Gottfried Wilhelm Leibniz and Seki Kōwa.

Calculus – Isaac Newton, Gottfried Wilhelm Leibniz, Pierre de Fermat and others.<sup>[22]</sup>

Newton–Raphson method – Joseph Raphson (1690), Isaac Newton (Newton's work was written in 1671, but not published until 1736).

Brachistochrone problem solved by Johann Bernoulli, Jakob Bernoulli, Isaac Newton, Gottfried Wilhelm Leibniz, Guillaume de l'Hôpital, and Ehrenfried Walther von Tschirnhaus. The problem was posed in 1696 by Johann Bernoulli, and its solutions were published next year.

Complex plane – Geometrical representation of complex numbers was discovered independently by Caspar Wessel (1799), Jean-Robert Argand (1806), John Warren (1828), and Carl Friedrich Gauss (1831).<sup>[28]</sup>

Non-Euclidean geometry (hyperbolic geometry) – Nikolai Ivanovich Lobachevsky (1830), János Bolyai (1832); preceded by Gauss (unpublished result) ca. 1805.

The list goes on and on....